# NCERT SOLUTIONS CLASS-8 MATHS CHAPTER-3 EXERCISE-3.3

1. Given a parallelogram ABCD. Complete each statement along with the definition or property used.

(i) AD = ..... (ii)  $\angle DCB$  = .....

(iii) OC = ..... (iv)  $\angle DAB + \angle CDA = ....$ 

#### **Answer**

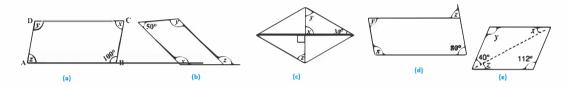
(i) AD = BC (Opposite sides of a parallelogram are equal)

(ii)  $\angle DCB = \angle DAB$  (Opposite angles of a parallelogram are equal)

(iii) OC = OA (Diagonals of a parallelogram are equal)

(iv) m  $\angle DAB$  + m  $\angle CDA$  = 180°

2. Consider the following parallelograms. Find the values of the unknowns x, y, z.



#### **Answer**

(a)



 $y = 100^{\circ}$  (opposite angles of a parallelogram)

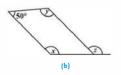
 $x + 100^{\circ} = 180^{\circ}$  (Adjacent angles of a parallelogram)

$$\Rightarrow x = 180^{\circ} - 100^{\circ} = 80^{\circ}$$

 $x = z = 80^{\circ}$  (opposite angles of a parallelogram)

Thus,  $x = 80^{\circ}$ ,  $y = 100^{\circ}$  and  $y = 100^{\circ}$ 

(b)

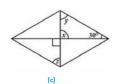


 $50^{\circ} + x = 180^{\circ} \Rightarrow x = 180^{\circ} - 50^{\circ} = 130^{\circ}$  (Adjacent angles of a parallelogram)

 $x = y = 130^{\circ}$  (opposite angles of a parallelogram)

 $x = z = 130^{\circ}$  (corresponding angle)

(c)



$$\Rightarrow 90^{\circ}$$
 + y +  $30^{\circ}$  =  $180^{\circ}$ 

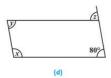
$$\Rightarrow$$
 y =  $180^{\circ}$  –  $120^{\circ}$  =  $60^{\circ}$ 

also, 
$$y = z =$$

 $60^{\circ}$ 

(alternate angles)

(d)



 $z = 80^{\circ}$  (corresponding angle)

$$z = y = 80^{\circ}$$
 (alternate angles)

$$x + y = 180^{\circ}$$
 (adjacent angles)

$$\Rightarrow$$
 x + 80° = 180°  $\Rightarrow$  x 180° - 80° = 100°

(e)



y =  $112^{\circ}$  [Opposite angles are equal in a parallelogram

$$40^{\circ} + y + x = 180^{\circ} 40^{\circ} + 112^{\circ} + x = 180^{\circ} 152^{\circ} + x = 180^{\circ} x = 180^{\circ} - 152^{\circ} = 28^{\circ}$$

and 
$$z = x = 28^{\circ}$$
 [Alternate angles]

#### 3. Can a quadrilateral ABCD be a parallelogram if

(i) 
$$\angle D$$
 +  $\angle B$  =  $180^{\circ}$ ? (ii) AB = DC = 8 cm, AD = 4 cm and BC = 4.4 cm?

(iii) 
$$\angle A = 70^{\circ}$$
 and  $\angle C = 65^{\circ}$ ?

#### Answer

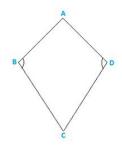
(i)Yes, a quadrilateral ABCD be a parallelogram if  $\angle D$  +  $\angle B$  =  $180^{\circ}$  but it should also fulfilled some conditions which are:

The sum of the adjacent angles should be  $180^\circ$ 

Opposite angles must be equal.

- (ii) No, opposite sides should be of same length. Here, AD ≠ BC
- (iii) No, opposite angles should be of same measures.  $\angle A \neq \angle C$

4. Draw a rough figure of a quadrilateral that is not a parallelogram but has exactly two opposite angles of equa measure.



#### Answer

ABCD is a figure of quadrilateral that is not a parallelogram but has exactly two opposite angles that is  $\angle B = \angle D$  of equal measure. It is not a parallelogram because  $\angle A \neq \angle C$ 

5. The measures of two adjacent angles of a parallelogram are in the ratio 3 : 2. Find the measure of each of the angles of the parallelogram.

#### Answer

Let the measures of two adjacent angles  $\angle A$  and  $\angle B$  be 3x and 2x respectively in parallelogram ABCD.

$$\angle A$$
 +  $\angle B$  = 180°

$$\Rightarrow$$
 3x + 2x =  $180^{\circ}$ 

$$\Rightarrow$$
 5x = 180°

$$\Rightarrow$$
 x =  $36^{\circ}$ 



We know that opposite sides of a parallelogram are equal.

$$\angle A = \angle C = 3x = 3 \times 36^{\circ} = 108^{\circ}$$

$$\angle B = \angle D = 2x = 2 \times 36^{\circ} = 72^{\circ}$$

6. Two adjacent angles of a parallelogram have equal measure. Find the measure of each of the angles of the parallelogram.

#### Answer

Let ABCD be a parallelogram.

Sum of adjacent angles of a parallelogram =  $180^{\circ}$ 

$$/A + /B = 180^{\circ}$$

$$\Rightarrow 2\angle A = 180^{\circ}$$

$$\Rightarrow \angle A = 90^{\circ}$$

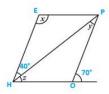
also, 
$$90^{\circ}$$
 +  $\angle B = 180^{\circ}$ 

$$\Rightarrow \angle B = 180^{\circ} - 90^{\circ} = 90^{\circ}$$

$$\angle A = \angle C = 90^{\circ}$$

## 7. The adjacent figure HOPE is a parallelogram. Find the angle measures x, y and z. State the properties you use to find them.

#### Answer



y =  $40^{\circ}$  (alternate interior angle)

 $\angle P$  =  $70^{\circ}$  (alternate interior angle)

 $\angle P = \angle H = 70^{\circ}$  (opposite angles of a parallelogram)

$$z = \angle H - 40^{\circ} = 70^{\circ} - 40^{\circ} = 30^{\circ}$$

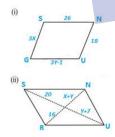
$$\angle H$$
 + x =  $180^{\circ}$ 

$$\Rightarrow$$
70° + x = 180°

$$\Rightarrow$$
 x = 180° - 70° = 110°



8. The following figures GUNS and RUNS are parallelograms. Find x and y. (Lengths are in cm)



#### Answer

(i) SG = NU and SN = GU (opposite sides of a parallelogram are equal)

$$3x = 18$$

$$\Rightarrow$$
 x = 18/3 = 6

$$3y - 1 = 26$$
 and,

$$\Rightarrow$$
 3y = 26 + 1

$$\Rightarrow$$
 y = 27/3 = 9

$$x = 6$$
 and  $y = 9$ 

$$y + 7 = 20$$

$$\Rightarrow$$
 y = 20 - 7 = 13 and,

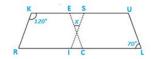
$$x + y = 16$$

$$\Rightarrow$$
 x + 13 = 16

$$\Rightarrow$$
 x = 16 - 13 = 3

$$x = 3$$
 and  $y = 13$ 

9. In the below figure both RISK and CLUE are parallelograms. Find the value of x.



#### Answer

 $\angle K$  +  $\angle R$  = 180° (adjacent angles of a parallelogram are supplementary)

$$\Rightarrow 120^{\circ} + \angle R = 180^{\circ}$$

$$\Rightarrow \angle R = 180^{\circ} - 120^{\circ} = 60^{\circ}$$

also,  $\angle R = \angle SIL$  (corresponding angles)

$$\Rightarrow \angle SIL = 60^{\circ}$$

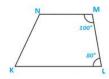
also,  $\angle ECR$  =  $\angle L$  =  $70^{\circ}$  (corresponding angles)

 $x + 60^{\circ} + 70^{\circ} = 180^{\circ}$  (angle sum of a triangle)

$$\Rightarrow$$
 x + 130 $^{\circ}$  = 180 $^{\circ}$ 

$$\Rightarrow$$
 x = 180° - 130° = 50°

10. Explain how this figure is a trapezium. Which of its two sides are parallel? (Fig 3.32)



#### Answer

When a transversal line intersects two lines in such a way that the sum of the adjacent angles on the same side of transversal is  $180^{\circ}$ 

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then the lines are parallel to each other.

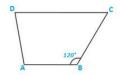
Here, 
$$\angle M$$
 +  $\angle L$  =100°

Thus, MN || LK

As the quadrilateral KLMN has one pair of parallel line therefore it is a trapezium.

MN and LK are parallel lines.

#### 11. Find m $\angle C$ in Fig 3.33 if AB || DC ?



#### Answer

$$m\angle C + m\angle B = 180^{\circ}$$

(angles on the same side of transversal)

$$\Rightarrow$$
m $\angle C + 60^{\circ}$ 

 $= 180^{\circ}$ 



 $-60^{\circ}$ 

 $= 120^{\circ}$ 

### 12. Find the measure of $\angle p$ and $\angle S$ if SP $\parallel$ RQ ? in Fig 3.34. (If you find m $\angle R$ , is there more than one method to find m $\angle p$ ?)



#### Answer

$$\angle p$$
 + $\angle Q$  =  $180^{\circ}$ 

(angles on the same side of transversal)

$$\Rightarrow \angle p +130^{\circ} = 180^{\circ}$$

$$-130^{\circ} = 50^{\circ}$$

also, 
$$\angle R + \angle S = 180^{\circ}$$

(angles on the same side of transversal)

$$\Rightarrow 90^{\circ} + \angle S = 180^{\circ}$$

$$\Rightarrow \angle S = 180^{\circ}$$

$$-90^{\circ} = 90^{\circ}$$

Thus,  $\angle p$  =50° and  $\angle S$  = 90°

Yes, there are more than one method to find  $\mathsf{m} \angle p$  .

PQRS is a quadrilateral. Sum of measures of all angles is  $360^\circ$ 

Since, we know the measurement of  $\angle Q$  , $\angle R$  and  $\angle S$  .

$$\angle Q$$
 =  $130^{\circ}$ ,  $\angle R$  =  $90^{\circ}$  and  $\angle S$  =  $90^{\circ}$ 

$$\angle p + 130^{\circ} + 90^{\circ} + 90^{\circ} = 360^{\circ}$$

$$\Rightarrow \angle p +310^{\circ} = 360^{\circ}$$

$$\Rightarrow \angle p$$
 =360°  $-310^{\circ}$  =  $50^{\circ}$ 

